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# 9th International Mathematics and Science Olympiad (IMSO) for Primary School 2012

### **Instructions:**

- \* Write down your name and country on the answer sheet.
- \* Write your answer on the answer sheet.
- \* You have 120 minutes to work on this test.
- \* Use pen or pencil to write your answer.



"Smart, Skilled, and Creative In a Joyful Competition for Excellence"

City Montessori Inter College, RDSO Campus, Manak Nagar, Lucknow, India 27 Oct. – 2 Nov 2012

#### **International Mathematics and Science Olympiad 2012**

### **EXPLORATION PROBLEMS**

1. Fill in the positive integers 1 to 30 into the following boxes to form 15 fractions, with each number used exactly once, such that as many of these fractions as possible have integer values.

$\Box$ '	$\Box$ ,	$\Box$ ,	$\Box$ ,	$\Box$ '	$\Box$ '	$\Box$ ,	$\Box$ '	$\overline{\Box}$ ,	$\overline{\Box}$ ,	$\overline{\Box}$ ,	$\overline{\Box}$ ,	$\Box$ '	$\Box$ '	

- 2. A palindrome number is a positive integer that can be read the same way in either direction. For instance, 909, 3553 and 12421 are palindrome numbers. Find all 5-digit palindrome numbers divisible by 44.
- 3. The plane is divided into a number of non-overlapping polygons by *n* lines. What is the largest number of triangles among these polygons?
  - (a) When n=5? (1 point)
  - (b) When *n*=6? (2 point)
  - (c) When *n*=7? (3 point)
- 4. Select as many of the integers from 1 to 21 as possible, so that no two disjoint pairs of them have the same difference. For example  $\{1, 3, 5, 13\}$  is such a collection; although 3-1=5-3, the two pairs are not disjoint. On the other hand,  $\{1, 2, 4, 7, 10\}$  is not since 4-1=10-7. What is the maximum number of integers that can be select?
- 5. Find a three-digit number such that the ratio of this three-digit number to the sum of its digit has the least value.
- 6. Place the numbers 1 to 42 in the squares of the  $6 \times 7$  table so that any two consecutive numbers are in squares which share a common side. The numbers 11, 20 and 30 are already placed as shown in the diagram below.

11	20		
30			

# **EXPLORATION PROBLEMS**

NAME	COUNTRY									
1. <b>Ans</b>	<b>Answer Sheet</b>									
2.										
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, ,	,,,,									
,,	· , , , , _ , _ ,									
3.										
(a) (b)	(c)									

# **EXPLORATION PROBLEMS**

NAME \_\_\_\_\_ COUNTRY \_\_\_\_\_

## **Answer Sheet**

4. The maximum number of integers that can be selected is \_\_\_\_\_\_.

5. The answer is \_\_\_\_\_.

6.

11	20		
30			