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International Young Mathematicians' Convention (IYMC) 2012 Individual Contest –Junior level



ANSWER SHEET

Name

Team

Candidate

Score

Code

number

Time: 60 minutes

Instructions:

- Write down your name, team code and candidate number on the answer sheet.
- Write down all answers on the answer sheet. Only **Arabic NUMERICAL** answers are needed.
- Answer all 8 problems. Each problem is worth 10 point and the total is 80 points.
- For problems involving more than one answer, points are given only when ALL answers are corrected.
- No calculator or calculating device is allowed.
- Answer the problems with pencil, blue or black ball pen.
- All materials will be collected at the end of the competition.

1	minutes	5	stones
2		6	
3		7	
4		8	0

International Young Mathematicians' Convention (IYMC) 2012 Individual Contest Junion level



- 1. A watch with an hour hand and a minute hand shows the time as 3:28. How many minutes later will the angle between the two hands be equal to 120°?
- 2. In the figure below, lines *AB*, *DE* and *CF* are perpendicular to line *BD*. If AB = 30 and DE = 20, find the length of *CF*.



- **3.** When 40! is expanded in base 10, what is the tenth digit from the right? (We define *n*! as the product of the integers from 1 to *n*.)
- 4. On a street, the houses are all on one side. They are numbered consecutively from 1 to 99. There is a value of x such that 3 times the sum of the numbers of the houses preceding the house numbered x is equal to the sum of the numbers of the houses following it. Find the value of x.
- 5. The total weight of several stones is 500 kilograms. The lightest ten stones weigh 200 kilograms. The heaviest six stones weigh 145 kilograms. The weights of stones are pairwise different and are not necessary integers. Find the number of stones.
- 6. Find the number of 10-digit numbers such that each of them is formed by using each of the digits 0 to 9 once, with no digit smaller than both neighbours.
- 7. A positive integer is said to be *curious* if it is the smallest of all positive integers with the same sum of digits. If all the *curious* numbers are arranged in ascending order, what is the 100^{th} number?
- 8. In triangle *ABC*, *AB* = *AC*. *D* is a point on *AC* and *E* is a point on *AB*. *BD* and *CE* intersect at *F*. If $\angle DBC = 50^{\circ}$, $\angle ABD = 30^{\circ}$, $\angle DCE = 20^{\circ}$ and $\angle ECB = 60^{\circ}$, what is the measure of $\angle CED$, in degree?

